

Table V. Deviations for 2600 Common Points

| combination of density correlation and mixing rule for T_{cm} | % av dev |
|---|----------|
| i modified Rackett equation with Chueh-Prausnitz mixing rule | 2.67 |
| ii generalized Guggenheim equation with (a) Chiu et al. mixing rule | 3.55 |
| (b) Li mixing rule | 3.32 |

Table VI. Summary of the Deviations for Polar Systems

| | density model | | | Halm and Stiel |
|----------------|--|---------|------------------|----------------|
| | generalized Guggenheim | Harmens | modified Rackett | |
| | (a) Chueh-Prausnitz (824) ^a | | | |
| (i) % av dev | 3.50 | 2.67 | 1.55 | 6.27 |
| (ii) % max dev | -23.30 | -26.63 | -20.75 | -70.50 |
| | (b) Harmens (830) ^a | | | |
| (i) % av dev | | 2.61 | | |
| (ii) % max dev | | -17.88 | | |
| | (c) Chiu et al. (826) ^a | | | |
| (i) % av dev | | 3.19 | | |
| (ii) % max dev | | -28.39 | | |

^a Mixing rule for pseudocritical temperature. The numbers in parentheses indicate the number of points.

V saturated liquid volume, cm³/g-mol
 x mole fraction
 Z_{RA} constant in modified Rackett equation

Subscripts

c critical value
 i, j components

ij $i-j$ binary interaction
 m mixture value
 r reduced value

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Vapor-Liquid Equilibrium Data for the Systems H₂O-H₂SO₄-HCl, H₂O-H₂SO₄-HBr, and H₂O-HBr at 780 mmHg Pressure

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With the help of a dynamic still made of tantalum, the liquid-vapor equilibria in the ternary systems H₂O-H₂SO₄-HCl and H₂O-H₂SO₄-HBr have been determined for the range of concentrations used in extractive distillation with sulfuric acid as solvent. Liquid-vapor equilibrium in the binary system H₂O-HBr has been determined for concentrations lower than that of the azeotrope. H₂ala's correlation is used to calculate the equilibrium compositions. Equilibrium temperatures are correlated with an empirical relation.

All the measurements found in the literature (1, 2) relating to isobaric liquid-vapor equilibrium of the system H₂O-H₂SO₄-HCl cover a very small range of low hydrogen acid mole fractions only. For the system H₂O-H₂SO₄-HBr no result has been published at this date.

The importance of the knowledge of phase equilibria, particularly for the design of extractive distillation columns destined to completely recover the hydracid by removing the azeotrope H₂O-HCl or H₂O-HBr in the presence of sulfuric acid as solvent, has involved us in determining liquid-vapor equilibria in the two ternary systems H₂O-H₂SO₄-HBr and H₂O-H₂SO₄-HCl. The equilibrium of the binary H₂O-HBr has been also determined for concentrations lower than that of the azeotrope.

Experimental Method

Liquid-vapor equilibria are realized with the help of a dynamic Aubry-Gilot' pattern still (3). It consists of a tantalum coil mounted in a vessel through which circulates a thermoregulated fluid. The investigated solution passes continuously through the tantalum coil at a rate which permits sufficient contact time to establish thermal and phase equilibrium. At the outlet, the liquid

Table I. Vapor-Liquid Equilibrium Data at 780 mmHg Pressure for the System $H_2O-H_2SO_4-HCl$

| X_2 | X_1 | Y_1 | $t_b/^\circ C$ |
|--------|--------|--------|----------------|
| 0.0813 | 0.0569 | 0.1922 | 112.2 |
| 0.0936 | 0.0314 | 0.0810 | 113.2 |
| 0.0965 | 0.0567 | 0.3143 | 110.9 |
| 0.1008 | 0.0325 | 0.1108 | 113.8 |
| 0.1067 | 0.0442 | 0.2664 | 113.5 |
| 0.1163 | 0.0430 | 0.3378 | 112.4 |
| 0.1181 | 0.0353 | 0.2590 | 115.8 |
| 0.1229 | 0.0330 | 0.2630 | 115.6 |
| 0.1253 | 0.0387 | 0.3521 | 113.2 |
| 0.1274 | 0.0278 | 0.2275 | 117.0 |
| 0.1292 | 0.0439 | 0.4707 | 106.6 |
| 0.1359 | 0.0328 | 0.3593 | 112.8 |
| 0.1363 | 0.0283 | 0.3018 | 116.9 |
| 0.1365 | 0.0472 | 0.6165 | 104.1 |
| 0.1391 | 0.0400 | 0.5240 | 105.9 |
| 0.1395 | 0.0364 | 0.4883 | 110.9 |
| 0.1406 | 0.0377 | 0.5126 | 107.7 |
| 0.1467 | 0.0211 | 0.2666 | 119.7 |
| 0.1489 | 0.0225 | 0.3005 | 119.0 |
| 0.1507 | 0.0294 | 0.4898 | 112.5 |
| 0.1532 | 0.0278 | 0.5003 | 112.7 |
| 0.1541 | 0.0244 | 0.3829 | 115.5 |
| 0.1543 | 0.0271 | 0.4939 | 112.8 |
| 0.1563 | 0.0335 | 0.6161 | 106.0 |
| 0.1569 | 0.0162 | 0.2657 | 121.0 |
| 0.1585 | 0.0355 | 0.7082 | 104.3 |
| 0.1607 | 0.0244 | 0.4891 | 114.5 |
| 0.1609 | 0.0212 | 0.4493 | 114.8 |
| 0.1696 | 0.0209 | 0.5281 | 113.6 |
| 0.1654 | 0.0255 | 0.5552 | 109.6 |
| 0.1674 | 0.0232 | 0.5371 | 111.0 |
| 0.1696 | 0.0153 | 0.3549 | 117.7 |
| 0.1743 | 0.0106 | 0.2958 | 121.3 |
| 0.1747 | 0.0177 | 0.5056 | 115.8 |
| 0.1775 | 0.0109 | 0.3141 | 121.0 |
| 0.1790 | 0.0134 | 0.4025 | 117.1 |
| 0.1818 | 0.0077 | 0.2368 | 123.1 |
| 0.1822 | 0.0112 | 0.3152 | 119.1 |
| 0.1827 | 0.0156 | 0.5075 | 115.0 |
| 0.1852 | 0.0271 | 0.8601 | 105.0 |
| 0.1866 | 0.0136 | 0.4409 | 116.7 |
| 0.1870 | 0.0199 | 0.6479 | 108.6 |
| 0.1891 | 0.0112 | 0.3189 | 118.4 |
| 0.1893 | 0.0200 | 0.7227 | 107.8 |
| 0.1903 | 0.0171 | 0.5931 | 110.0 |
| 0.1926 | 0.0146 | 0.5904 | 111.9 |

and vapor phases are separated and analyzed. The temperature and the pressure are measured in the separator. The temperature is read on a METRIX PX 2000 digital Pt resistance thermometer with an accuracy of $\pm 0.1^\circ C$. The pressure in the still is balanced by an external pressure of nitrogen by means of a differential U-tube manometer (precision ± 0.5 mmHg) and measured with a Texas Instruments precision pressure gauge (Model 145) equipped with a fused quartz Bourdon capsule (precision ± 0.1 mmHg). The accuracy of the pressure measured in the equilibrium still is therefore better than ± 1 mmHg. The temperature of the thermoregulated fluid is adjusted to work under isobaric conditions; a pressure slightly higher than the atmospheric pressure is established in order to balance out variations in this quantity and pressure drops in the apparatus.

As regards the analyses, the total acid content was measured by titration with 0.1 N NaOH, and the concentration of Cl^- or Br^- was measured with a potentiometric system using a silver electrode. The mole fractions are so determined with an accuracy of $\pm 5 \times 10^{-4}$.

Results and Discussion

Ternaries $H_2O-H_2SO_4-HCl$ and $H_2O-H_2SO_4-HBr$. By use of experimental points such as reported here (Tables I and II), the validity of Hála's model (4) has been examined for describing

Table II. Vapor-Liquid Equilibrium Data at 780 mmHg Pressure for the System $H_2O-H_2SO_4-HBr$

| X_2 | X_1 | Y_1 | $t_b/^\circ C$ |
|--------|--------|--------|----------------|
| 0.1457 | 0.0491 | 0.1277 | 131.0 |
| 0.1514 | 0.0584 | 0.2642 | 130.7 |
| 0.1632 | 0.0210 | 0.0190 | 130.4 |
| 0.1689 | 0.0266 | 0.0306 | 132.6 |
| 0.1700 | 0.0200 | 0.0191 | 132.3 |
| 0.1733 | 0.0435 | 0.2243 | 132.7 |
| 0.1757 | 0.0399 | 0.1825 | 133.4 |
| 0.1777 | 0.0364 | 0.0196 | 133.7 |
| 0.1814 | 0.0584 | 0.4225 | 124.6 |
| 0.1849 | 0.0490 | 0.4038 | 129.7 |
| 0.1897 | 0.0150 | 0.0258 | 135.4 |
| 0.1903 | 0.0254 | 0.1203 | 136.7 |
| 0.1918 | 0.0412 | 0.4032 | 132.2 |
| 0.1984 | 0.0215 | 0.1205 | 137.9 |
| 0.2010 | 0.0201 | 0.1317 | 138.1 |
| 0.2033 | 0.0420 | 0.4630 | 128.9 |
| 0.2046 | 0.0367 | 0.4036 | 132.7 |
| 0.2074 | 0.0368 | 0.4310 | 131.7 |
| 0.2084 | 0.0362 | 0.4289 | 132.6 |
| 0.2113 | 0.0300 | 0.3458 | 135.6 |
| 0.2142 | 0.0467 | 0.6200 | 121.0 |
| 0.2197 | 0.0315 | 0.4472 | 133.3 |
| 0.2204 | 0.0169 | 0.1443 | 141.0 |
| 0.2176 | 0.0200 | 0.1824 | 140.0 |
| 0.2187 | 0.0119 | 0.1162 | 140.8 |
| 0.2219 | 0.0280 | 0.4223 | 135.4 |
| 0.2223 | 0.0423 | 0.5980 | 123.2 |
| 0.2225 | 0.0317 | 0.1381 | 141.8 |
| 0.2225 | 0.0315 | 0.4752 | 133.1 |
| 0.2248 | 0.0246 | 0.3870 | 136.9 |
| 0.2252 | 0.0313 | 0.4951 | 132.5 |
| 0.2269 | 0.0120 | 0.1343 | 143.2 |
| 0.2277 | 0.0206 | 0.2753 | 139.0 |
| 0.2280 | 0.0294 | 0.4898 | 133.5 |
| 0.2283 | 0.0167 | 0.1856 | 142.0 |
| 0.2310 | 0.0228 | 0.4162 | 137.0 |
| 0.2338 | 0.0157 | 0.2280 | 143.5 |
| 0.2356 | 0.0182 | 0.3459 | 138.8 |
| 0.2375 | 0.0098 | 0.1101 | 146.1 |
| 0.2419 | 0.0128 | 0.2267 | 146.2 |
| 0.2425 | 0.0141 | 0.2819 | 145.3 |
| 0.2438 | 0.0121 | 0.2229 | 146.3 |
| 0.2448 | 0.0157 | 0.4187 | 139.7 |
| 0.2483 | 0.0218 | 0.5196 | 134.4 |
| 0.2474 | 0.0091 | 0.1732 | 147.7 |
| 0.2508 | 0.0222 | 0.5698 | 131.5 |
| 0.2508 | 0.0210 | 0.5216 | 133.5 |
| 0.2504 | 0.0107 | 0.2119 | 146.7 |
| 0.2523 | 0.0185 | 0.5021 | 136.4 |
| 0.2524 | 0.0200 | 0.5215 | 134.6 |
| 0.2528 | 0.0159 | 0.4681 | 138.2 |
| 0.2556 | 0.0177 | 0.5028 | 135.7 |
| 0.2624 | 0.0159 | 0.5023 | 135.9 |
| 0.2639 | 0.0127 | 0.4584 | 139.0 |
| 0.2695 | 0.0069 | 0.2766 | 148.8 |
| 0.2867 | 0.0109 | 0.6382 | 136.6 |
| 0.2923 | 0.0057 | 0.2587 | 150.3 |

Table III. Coefficients of Equation 2

| system | A | B | C | D |
|-------------------------|---------|---------|---------|---------|
| HCl- H_2SO_4 - H_2O | 43.073 | -29.297 | -39.163 | 35.826 |
| HBr- H_2SO_4 - H_2O | -63.187 | 108.28 | 30.784 | -39.325 |

the liquid-vapor equilibria of electrolytic solutions. According to Hála, eq 1 defines the relative pseudovolatility β_{13} of the hydrochloric acid with regard to water in the presence of sulfuric acid (whose concentration in the vapor phase is negligible).

$$\beta_{13} = \frac{Y_1}{1 - Y_1} \frac{X_3(1 + X_1 + X_2)}{X_1(X_1 + X_2)} \quad (1)$$

Assuming that the excess Gibbs energy of the solution can

Table IV. Vapor-Liquid Equilibrium Data at 780 mmHg Pressure for the System H₂O-HBr

| X_1 | Y_1 | $t_b/^\circ\text{C}$ |
|--------|--------|----------------------|
| 0.0866 | 0.0006 | 110.5 |
| 0.0957 | 0.0014 | 112.2 |
| 0.1037 | 0.0034 | 114.7 |
| 0.1134 | 0.0099 | 116.7 |
| 0.1193 | 0.0113 | 117.6 |
| 0.1245 | 0.0187 | 118.8 |
| 0.1273 | 0.0243 | 119.7 |
| 0.1351 | 0.0348 | 121.1 |
| 0.1421 | 0.0424 | 121.9 |
| 0.1460 | 0.0659 | 122.9 |
| 0.1551 | 0.1173 | 124.2 |
| 0.1676 | 0.1676 | 124.7 |

be expressed with a series expansion in terms of the ionic strength of the solution and keeping only the first three terms of the series, one obtains the relation

$$\ln \beta_{13} = A + BI^{1/2} + C(1 - 2X_1 - X_2) + DX_2 \quad (2)$$

where $I = X_1 + X_2$.

The coefficients of eq 2, determined by linear regression, are given in Table III.

For these calculations, only the first dissociation of the sulfuric acid is taken into account since the concentration of SO_4^{2-} ions is completely negligible in view of the high acidity of the solution.

In addition, it should be observed that small errors in the experimental determination of the compositions lead to very important relative error for the coefficient of relative volatility

Table V. Coefficients of Equation 3

| system | a | b | c | d | e | f | std dev ($^\circ\text{C}$) |
|--|---------|--------|---------|--------|---------|---------|------------------------------|
| H ₂ O-H ₂ SO ₄ -HCl | 63.740 | 1126.1 | -3183.2 | 642.89 | -1582.7 | -9909.8 | 3.0 |
| H ₂ O-H ₂ SO ₄ -HBr | -74.292 | 3668.9 | -12059 | 1666.8 | -3069.3 | -16556 | 1.5 |

β_{13} in the range of low concentrations (although in theory, Hála's correlation has to be restricted to dilute solutions only). On the other hand, for high concentrations, the equilibrium is not as well represented by Hála's correlation, but the relative error of β_{13} is much lower.

Binary H₂O-HBr. As regards the binary system H₂O-HBr, the comparison between the results of the present work (Table IV) and that of Carriere and Cerveau (5) shows a good agreement on the boiling curve (Figure 1), however with slight deviation for the azeotropic temperature. As to the dew-point curve, higher values are obtained in the range of lower concentrations.

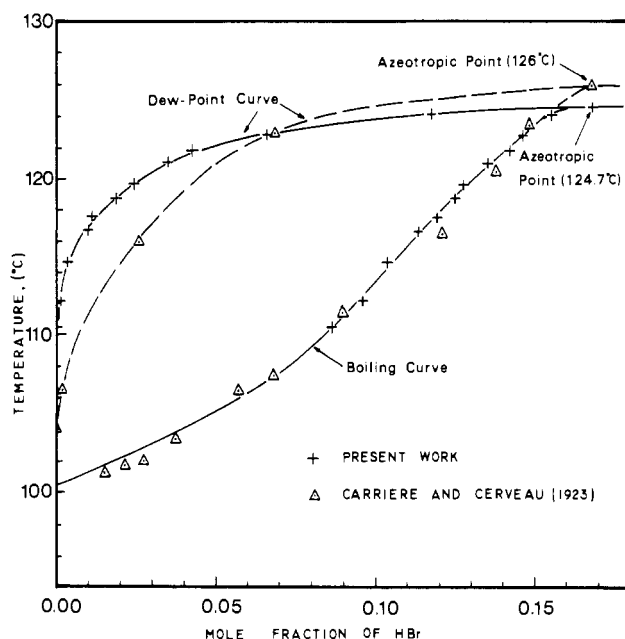
Boiling Temperatures. The experimental boiling temperatures were correlated with a multilinear regression giving the coefficients of the equation

$$t_b/^\circ\text{C} = a + bX_1 + cX_1^2 + dX_2 + eX_2^2 + fX_1X_2 \quad (3)$$

The coefficients obtained are given in Table V for the two ternary systems.

The ranges of validity are the following: with HCl, $0 < X_1 < 0.06$, $0.10 < X_2 < 0.22$; with HBr, $0 < X_1 < 0.05$, $0.18 < X_2 < 0.27$.

Nevertheless, the values obtained remain correct even outside the range of validity given above. These equations have no

Figure 1. Temperature-composition diagram for the H₂O-HBr system at 780 mmHg pressure.

theoretical background but are very useful for computer programs.

Glossary

| | |
|---------|---------------------------------------|
| β | Hála coefficient |
| I | ionic strength |
| X | mole fraction in liquid |
| Y | mole fraction in vapor |
| t_b | boiling temperature, $^\circ\text{C}$ |

Subscripts

| | |
|---|---------------------------------------|
| 1 | hydrochloric acid or hydrobromic acid |
| 2 | sulfuric acid |
| 3 | water |

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